

Wave Behaviour of Particles Assignment SOLUTIONS

1.

a) $p = \frac{h}{\lambda}$ (or) $\lambda = \frac{h}{p}$

Particles exhibit a wavelength inversely proportional to their momentum

b) $m = m_{\alpha} = 6.645 \times 10^{-27} \text{ kg}$

$$\lambda = \frac{h}{p} = \frac{h}{mv} = \frac{6.63 \times 10^{-34}}{6.645 \times 10^{-27} \times 1.67 \times 10^7} = 5.97 \times 10^{-15} \text{ m}$$

2.

a) Should be *smooth* curve that does not tightly fit all points, just shows the general wavy pattern

b) $\sim 50^\circ$

c) The maximum intensity indicates an interference maxima. It can therefore be inferred that electrons exhibit wave behaviour.

d) $d \sin \theta = m\lambda$

$$\begin{aligned} \therefore \lambda &= \frac{d \sin \theta}{m} \\ &= \frac{0.909 \times 10^{-9} \times \sin 50^\circ}{1} \\ &= 7 \times 10^{-10} \text{ m (1 s.f.)} \end{aligned}$$

e) $E = \frac{1}{2}mv^2$

$$\therefore mE = \frac{1}{2}m^2v^2$$

$$\therefore mE = \frac{1}{2}p^2$$

$$\therefore p = \sqrt{2mE}$$

$$m = 9.11 \times 10^{-31} \text{ kg} \quad E = 3 \times 1.60 \times 10^{-19} = 4.8 \times 10^{-19} \text{ J}$$

$$\therefore p = \sqrt{2 \times 9.11 \times 10^{-31} \times 4.8 \times 10^{-19}} = 9.35 \times 10^{-25} \text{ kgms}^{-1}$$

According to de Broglie's relation:

$$\lambda = \frac{h}{p} = \frac{6.63 \times 10^{-34}}{9.35 \times 10^{-25}} = 7 \times 10^{-10} \text{ m (1 s.f.)}$$

Since this is the same as the experimental result, de Broglie's relation is verified.

3. Higher resolution, because of smaller wavelength

Higher magnification, because electric/magnetic fields are used instead of glass