## Circular Motion, Gravitation and Satellites

1. The Earth travels around the Sun in a roughly circular path at a constant speed.
a) Explain how the Earth can be accelerating, even though its speed is not changing.
b) Identify the force causing the Earth's acceleration.
2. An skateboarder of mass $m=60 \mathrm{~kg}$ is attached to a rope, and is moving with uniform circular motion.

The length of the rope attached to the skateboarder is $r=10 \mathrm{~m}$, as shown in the diagram below. The period of the skateboarder's circular motion about point X is 6.28 s .
Ignore any effects of gravity or friction.

a) Identify the force that is causing the centripetal acceleration of the skateboarder.
b) Show that the magnitude of the tension $F$ in the rope is given by $F=\frac{4 \pi^{2} m r}{T^{2}}$.
c) Hence calculate the magnitude of the tension in the rope.
3. The curves on many roads carrying high-speed traffic are banked.
a) With the aid of a diagram, explain how banking a curve decreases the reliance upon friction between the tyres and the road.
b) Hence show that the relationship between the banking angle, the speed of a car and the radius of the curve when no centripetal acceleration is provided by friction can be given by $\tan \theta=\frac{v^{2}}{r g}$.
4. Two satellites are orbiting different planets, but both with the same radius of orbit around their planet. Satellite 1 is orbiting Planet 1 with speed $1552 \mathrm{~ms}^{-1}$. Planet 2, which Satellite 2 is orbiting, has four times the mass of Planet 1.
a) Using proportionality, determine the orbital speed of Satellite 2 around Planet 2.
b) Explain why the centre of a satellite's orbit must coincide with the centre of mass of the planet. Assume the satellite's orbit around the planet is circular.
5. Explain the advantage of launching low-altitude equatorial-orbit satellites in a west-to-east direction.
6. State and explain whether a geosynchronous (geostationary) orbit or a low-altitude polar orbit would be more appropriate for a meteorology and surveillance satellite.

