## Question 10 (10 marks)



Figure 10 shows an Argand diagram superimposed on an aerial photograph.

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## Figure 10

(a) Write an inequality that represents all complex numbers z in the region bounded by, and including, the circle.

(2 marks)

- (b) (i) On Figure 10, mark the position of the complex number 3 + 4i with an X. (1 mark)
  - (ii) Show that any point on the straight line through the origin (*O*) and *X* has the form 3t + 4it, where *t* is a real parameter.

(1 mark)

(c) (i) If z is any point in the region bounded by, and including, the circle, apply the triangle inequality to the triangle that has vertices at z, X, and O to show that

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\left|z-\left(3+4i\right)\right|\leq 7.
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## (2 marks)

- (ii) On Figure 10, on the region bounded by, and including, the circle, mark the point *P* for which |z (3 + 4i)| = 7. (1 mark)
- (d) Using part (b)(ii) or otherwise, find the complex number that is represented by *P*.



(2 marks)

(e) A mobile phone tower at *O* provides reception for 2 km in any direction. A new tower is going to be built at *X*, which will provide reception for 7 km in any direction.

Explain why the tower at *O* will not be needed, once a tower is built at *X*.

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(1 mark)